

科目名稱	材料力學	類組代碼	D37
		科目碼	D3793

※本項考試依簡章規定所有考科均「不可」使用計算機。

本科試題共計 1 頁

1. A steel pipe of thickness  $t_s$  and an aluminum pipe of thickness  $t_a$  are securely bonded together to form a composite cylinder. The aluminum pipe has an inner radius  $r_o$ , and the cross-section of the composite cylinder is shown in Fig.1. For the steel, the Young's modulus is  $E_s$  and the Poisson's ratio is  $\nu_o$ , while for the aluminum, the Young's modulus is  $E_a$  and the Poisson's ratio is also  $\nu_o$ .

(a) Given that the composite cylinder is subjected to a force  $P$  applied at the origin along the positive  $x$ -axis, determine the maximum stress in both the aluminum and the steel, as well as the change in the inner radius of the steel. (20%)

(b) Given that the composite cylinder is subjected to a force  $P$  applied at  $y = r_o$  along the positive  $x$ -axis, determine the maximum stress in both the aluminum and the steel. (15%)

(c) Given that the composite cylinder is subjected to a force  $P$  applied at  $y = r_o$  along the positive  $z$ -axis and another force  $P$  applied at  $y = -r_o$  along the negative  $z$ -axis, determine the maximum stress in both the aluminum and the steel. (15%)

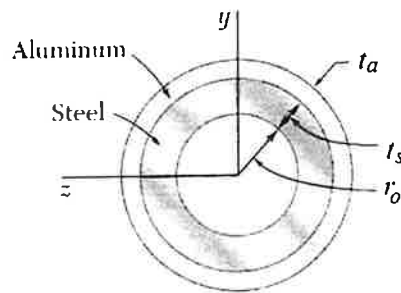


Fig. 1

2. A beam AB of length  $L$ , width  $b$  and height  $h$  undergoes a temperature change such that the top of the beam is at temperature  $T_1$  and the bottom of the beam is at temperature  $T_2$ . Assume that the beam AB has an elastic modulus  $E$  and a thermal expansion coefficient  $\alpha$ .

(a) If the beam AB is simply supported, as shown in Fig.2(a), and  $T_1 > T_2$ , find the maximum deflection of the beam and the reactions at supports A and B. (15%)

(b) If both ends A and B are fixed, as shown in Fig.2(b), and  $T_1 = T_2$ , find the maximum deflection of the beam and the reactions at the ends A and B. (15%)

(c) If both ends A and B are both fixed, as shown in Fig.2(b), and  $T_1 < T_2$ , find the maximum deflection of the beam and the reactions at the ends A and B. (20%)

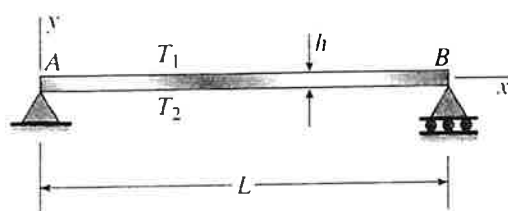


Fig.2(a)

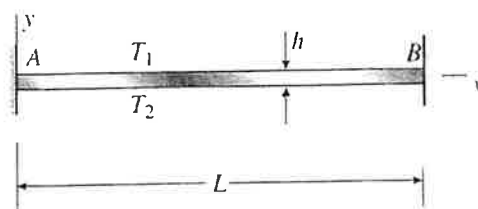


Fig.2(b)